Wireless Schedulers with Future Sight via Real-Time 3D Environment Mapping

Matthew Webb, Congzheng Han, Angela Doufexi, and Mark Beach
University of Bristol, UK. Email: {M.W.Webb, Bernice.Han, A.Doufexi, M.A.Beach}@bristol.ac.uk

Abstract—This paper proposes a new wireless scheduling methodology which takes advantage of future predictions of data rate for the several users competing for physical access. Based on a system which allows low-cost 3D mapping of an environment in real-time, the predictions are obtained via either low-resolution ray-tracing based on simple path-loss prediction given the physical structure of the surroundings or by reference to data rates achieved by previous visitors to a locality. The proportional fair scheduling (PFS) metric is extended to include measures of the future rates users may achieve, leading to a new family of schedulers. They show useful fairness improvements over PFS in exchange for a small capacity loss, and allow a number of configuration options and a range of trade-offs between fairness and capacity.

I. INTRODUCTION

The physical structure of the environment around a wireless network has for many years been used to enable ray-tracing for analysis and design, e.g. Layar [3] and the ViewNet project [4]. In ViewNet’s system, on which this paper’s work is based, mobile operatives carry a webcam whose video stream is processed by a visual simultaneous localization and mapping (VSLAM) application to identify points-of-interest in the environment [5], [6]. Coordinates for these points are determined by multi-lateration around the camera and reference to absolute positioning systems such as GPS. Points are grouped to identify physical objects, giving a structural map of the environment. Users send their maps to a central controller which fuses them into one which is available to users who are currently present or who arrive later.

This paper will use the information about future data rates available from such systems to suggest a new wireless scheduling methodology utilizing both the past information common to existing schedulers and also the future information available from augmented reality systems like ViewNet. Such a scheduler utilizes a class of information that is not normally available, so opening up new possibilities in scheduler design. The approach takes the scheduling metric used by the classical proportional fair scheduler (PFS), which relies on past and present data rate information, and augments it to include various measures of future data rates that users are expected to achieve. This leads to several different future-based schedulers, and they have a number of free parameters which influence their behavior and capacity–fairness tradeoffs.

The PFS has been examined in a related way in [7], where one of the schedulers used here is derived in part but in a different manner without the more general access to the scheduling metric which is the basis of this paper, and in [8] where future rates are considered on a probabilistic basis. Other predictive scheduling work includes [9] which is effectively a greedy search scheduler over some future time-slots, extended in [10] to consider the impact of re-configuring the system when the scheduler requires a change. An approach for a different family of scheduler is suggested in [11], which alters a simple scheduling metric to include future information in a way reminiscent of this paper, but for the very different metric they use, and less flexibly than here.

Section II introduces the main scheduling terminology and theory needed in Section III which sets out the theory of the future-based scheduling methodology that is the key contribution of the paper. Section IV presents numerical results showing the behavior of the various schedulers and finally Section V summarizes the paper and suggests future work.

II. CLASSICAL SCHEDULING

There are many criteria against which several competing users may be assessed to determine which should be granted access to a limited network resource (or ‘scheduled’) [12]. The two of interest here are throughput maximization (so-called ‘greedy’) scheduling as a baseline, and proportional fairness on which the new methodology presented in this paper is based.

Classical schedulers base their scheduling choices on a combination of the current and past values of data rate available to the users. If there are $K$ simultaneously competing users in the system, and user $k = 1, 2, \ldots, K$ has rate $R_k(t)$ at scheduling time $t$, then a scheduler assigns to each user a metric $m_k(t)$ and schedules the user $k^*(t) = \arg\max_k m_k(t)$.

A. Greedy Scheduler

A scheduler that chooses at each scheduling point the user with the highest throughput, the so-called ‘greedy’ scheduler,
is frequently used as a baseline comparison for other schedulers in wireless communication studies. The metric is simply:

\[ m_k(t) = R_k(t). \]  

Although this will maximize the throughput, it makes no particular attempt to share access to the network resource among the competing users. This question of fairness is considered in Section II-C. More sophisticated schedulers are therefore generally used.

**B. Proportional Fair Scheduler**

Originally described in [13], the proportional fair scheduler (PFS) began receiving attention in modern wireless studies in [14]. It grants access to the channel to the user whose prevailing channel conditions are best with respect to their average conditions. The PFS scheduling metric is:

\[ m_k(t) = \frac{R_k(t)}{T_k(t)}, \]  

where \( T_k(t) \) is the exponentially-weighted average of user \( k \)'s previous throughputs:

\[ T_k(t + 1) = \begin{cases} 
(1 - 1/t_c) T_k(t) + (1/t_c) R_k(t), & k = k^*, \\
(1 - 1/t_c) T_k(t), & k \neq k^*, 
\end{cases} \]

with \( t_c \) chosen to reflect the rate of change in the channel. Shorter \( t_c \) tends to make the system fairer among the \( K \) users but results in lower throughput compared to longer \( t_c \) which schedules more greedily but less fairly.

An important implication here is that the PFS, greedy scheduler, and the other classical schedulers form their metrics based only on the current rate and past rates since this is traditionally the only information that would be available. However, ViewNet offers access to predictions of future throughputs.

**C. Fairness**

Since a user will not be able to transmit at all times with the use of a scheduler, some measure of how fairly the available resources are divided up among the users is needed. A popular measure of fairness is Jain’s fairness index (JFI) [15]:

\[ J(t) = \frac{\left( \sum_{k=1}^{K} R_k(t) \right)^2}{K \sum_{k=1}^{K} R_k^2(t)}. \]

JFI has the property, among others, that \( 0 \leq J \leq 1 \), independently of \( K \) and the scale of \( R_k(t) \).

Since there is a loosely inverse relation between fairness and capacity, in Section IV results for both quantities will be presented. To provide some means of single-metric comparison between schedulers, a synthetic combined metric will also be used. Termined here the capacity-fairness product (CFP), and ‘capacity-fairness index’ in [16], it will be defined as:

\[ I(t) = R(t)J(t), \]

where \( R(t) \) is some suitable measure of the rate achieved by all scheduled users at time \( t \). In Section IV, this will be the mean rate of all scheduled users in an orthogonal frequency division multiple access (OFDMA) system. The CFP nominally has units bps/Hz, but this has no particular physical meaning.

**III. FUTURE-BASED SCHEDULING**

The proposal in this paper is to augment the scheduling metric in order to include some form of information about the future values of rate that the users will experience. Figure 1 shows the regions of interest along a given user’s rate curve assuming availability of estimates of future throughput values. The user is presently at time \( t = t_0 \). The exponential decay into the past informally represents the weight of the rates at times \( t \leq t_0 \) in the calculation of \( T_k(t) \) as a result of repeated application of (3). The window into the past more accurately extends over all \( 0 \leq t \leq t_0 \), but the window is shown bounded on the left to indicate the effect of the time scale \( t_c \).

The idea in this paper is to add to the PFS’s scheduling metric a weighted average of future throughputs in the numerator and/or denominator:

\[ m_k^F(t) = \frac{\alpha R_k(t) + \gamma F_k^N(t) + \delta F_k^D(t)}{\beta T_k(t) + \delta F_k^D(t)}, \]

where \( \alpha, \beta, \gamma, \delta \) can be any scalars and the two future-based functions \( F_k^N(t) \) and \( F_k^D(t) \) can be the same or different. The following possibilities are considered in this paper, where \( F_k(t) \) is shorthand for either of \( F_k^N(t) \) and \( F_k^D(t) \). The future track of \( R_k(t) \) is considered over \( N \) future scheduling points.

1) Future weighting: \( F_k(t) \) is an exponentially-decaying weighted average forwards from \( t_0 \), as \( T_k(t) \) is backwards:

\[ F_k^r(t) = (1/N) \sum_{n=1}^{N} (1 - 1/t_f) R_k(t + n). \]

This assigns most weight to throughputs that are in the near future and exponentially less to those further away. If \( F_k^N(t) = F_k^r(t) \) (denoted ‘FWD’), this function will reward high throughputs in the near term over those far away, whereas if \( F_k^D(t) = F_k^r(t) \) (denoted ‘FWD’), it will penalize them.
Both $N$ and $t_f$ are free parameters: $N$ controls how far into the future the scheduler assigns any weight at all to $R_k$, and $t_f$ is to the future what $t_c$ is to the past. Such a formulation fits the ViewNet scenario where it may be possible to predict a user’s track in the near future e.g. by extrapolating along a straight line from their recent track, but with less certainty at greater time lags. The fact that the summation is over all $n$ in the range has the implication that the user is allowed to transmit at all scheduling times. Whilst evidently over-optimistic, all users are at least treated in the same fashion.

2) Future sliding window: The second proposal is to actually compute $T_k(t)$ over both the past and future windows, again with the over-optimistic assumption that user $k$ transmits at all the $N$ future time-slots (denoted ‘TXA’). By repeated application of the $k = k^*$ portion of (3), the result is:

$$T_k(t + N) = (1 - 1/t_c)^N T_k(t) + \frac{1}{t_c} \sum_{n=1}^{N} (1 - 1/t_c)^{n-1} R_k(t + N - n).$$

This effectively has the reverse scheduling characteristics to the option discussed above, since $(1 - 1/t_c) < 1$. The expression in (8) can be viewed in the form of (6) with $\gamma = 0$:

$$\beta = \left(1 - \frac{1}{t_c}\right)^N \text{ and } F_k^D = \frac{1}{t_c} \sum_{n=1}^{N} (1 - 1/t_c)^{n-1} R_k(t + N - n),$$

and $\alpha$ any value, which view shows that the future measure is not necessarily confined to use in the denominator of (6) and also admits an additional scalar multiplier on $\beta$ if desired. This can also be combined with $F_k^N(t) = F_k^1(t)$ and $\gamma \neq 0$ from Section III-1, which will be denoted ‘FWN+TXA’.

3) Full Rescheduling over Future Window: The final proposal is a full re-scheduling at each of the $N$ future scheduling instants. That is, to slide the scheduler forwards, re-compute the scheduling at each slot and use this to produce, at the $N$th scheduling slot, a new estimate for $T_k$ which is then used directly in calculating $m_k(t)$. This avoids the ‘over-optimism’ of the previous two schedulers at the cost of clearly increased computational complexity. This requires no explicit future rate measure, so effectively $\gamma = \delta = 0$. This ‘full future’ scheduling is denoted ‘FFS’, and when combined with FWN in computing $m_k(t)$, ‘FFS+FWN’.

IV. Simulation Results

Results are shown in the context of a multiple-input multiple-output (MIMO) OFDMA system with the structure in Table I. A physical resource block (PRB) is a set of 16 adjacent subcarriers assigned to a single user. This groups the 768 data subcarriers into 48 PRBs. In what follows, each PRB is scheduled independently over time. The total capacity available to each user in a given PRB at time $t$ is used as $R_k(t)$. The future information is $R_k(t + n)$ at $n$ scheduling times into the future for the same PRB. The scheduling metrics for all users are updated at every step of $t$.

All users transmit a fixed power of 17 dBm and user $k$ experiences a received signal-to-noise ratio (SNR) based on their distance $d_k$ from the basestation (BS) in a 100 m radius circular cell. Path loss is based on the specifications in 802.11n [17]. These stipulate free space path-loss up to a breakpoint distance $d_b$ of 30 m and a path-loss index of 3.5 after this:

$$L_k(d_k) = \begin{cases} 46.4 + 20 \log_{10} d_k, & d_k < d_b \\ 46.4 + 20 \log_{10} d_b + 35 \log_{10} d_k/d_b, & d_k \geq d_b. \end{cases}$$

The fading channels are 3000 realizations of the ETSI BRAN ‘C’ model [18]. This represents a large open space (indoor or outdoor) in non-line of sight (NLOS) conditions.

A. Scheduler Characteristics

Figures 2–4 show the capacity, JFI and CFP characteristics of the eight scheduling possibilities with $t_c = t_f = N = 300$. Each is shown with five illustrative combinations of $\alpha$, $\beta$, $\gamma$, $\delta$, chosen to cover the observed differences in performance.

As would be expected, the greedy scheduler has the best capacity performance, and the others, since they are based on the PFS, have capacities in the region of that. It is apparent that there is some range of capacity performance available from the future-based schedulers, varying from 13.5 bps/Hz up to 16 bps/Hz, equivalent to the PFS. Clearly, FWN has the lowest capacity and FWN+TXA is the most sensitive to parameter changes, with $\alpha = \beta = 5; \gamma = \delta = 1$ giving slightly the highest capacity across the schedulers. These two schedulers both give a clear increase in JFI compared to the PFS, however, from an already-high 0.78 to 0.85–0.88 showing that addition of future rate measures to scheduling metrics is able to improve fairness over existing schedulers and maintains the significant gains of the PFS over rate-greedy scheduling.

The fairness improvement using the future measure in the numerator in FWN arises since it acts to smooth out temporary dips in rate by compensating for them in the scheduling metric with near-term increases in rate. A similar benefit is seen in the FWN+TXA combination, where the sensitivity results from both the numerator and denominator of (6) being affected, whereas the other schedulers only impact one or the other.

Haven if future measures in the denominator of $m_k(t)$ have less impact on capacity and fairness, as seen in the values for FWD and TXA, although TXA gives marginally the higher capacity and lower fairness. Adding terms to the denominator of $m_k(t)$ does not alter the fundamental nature of the metric.
in the way that adding to the numerator does, so the behavior
of such schedulers is very similar to the PFS. The more
complex ‘full-future scheduler’ has performance that matches
the PFS. The main effect of FFS is to produce a longer-term
average for $T$. The more
in the denominator of (6): the FFS schedules forwards on the
channel (and rate) are stationary then regardless of which
assumption that PFS scheduling decisions will be made, when
in fairness, and thus also reduces CFP. This is due to the
since it reduces capacity without any compensating increase
were in motion with mean path-loss changing over time.

The addition of FWN to FFS is undesirable in this scenario
since it reduces capacity without any compensating increase
in fairness, and thus also reduces CFP. This is due to the
disruption the FWN aspect causes to the PFS-equivalent FFS
in the denominator of (6): the FFS schedules forwards on the
assumption that FFS scheduling decisions will be made, when
in fact the decisions are based principally on FWN, and this
makes the FFS prediction of $T(t)$ incorrect. The FFS+FWN
combination thus chooses the ‘wrong’ users in some cases and
capacity tends to fall.

Using CFP as an indication of the overall change to behavior
between the schedulers in Fig. 4 shows that the product
performance is not changed significantly across most of the
scheduler options. This implies that the different balances in
capacity and fairness apparent in Figs. 2 and 3 can be achieved
with some transparency to the net tradeoff between the two.
This is particularly true of FWN and FWN+TXA where the
CFP is nearly the same as the other schedulers but a marked
fairness increase is available.

B. Effects of System Structure and Scheduler Parameters

A number of system parameters are considered in Figs. 5–7
to see their impact on performance and behavior.

Overall, these figures confirm that the future-based sched-

ules behave in ways familiar from classical scheduling theory,
with FWN and FWN+TXA retaining their fairness enhance-
ments. In particular, with the addition of more users, capacity
and fairness both decrease as there is increased competition for
the same bandwidth and PRBs. Encouragingly, none of them
show the same fairness degradation in this case as the greedy
scheduler. Further, as $t_c$ and $t_f$ are increased, the fairness falls
and capacity rises a little for the PFS and most of the future
schedulers, with an overall small fall in CFP. FFS+FWN,
however, shows a substantial loss in fairness as well as a
0.5 bps/Hz capacity loss and thus a CFP value some way below
the other future-based schedulers. The capacity loss arises as
identified previously; the fairness drop would arise anyway
but is compounded by that effect, resulting in the large drop
in fairness (and CFP) for the ‘10-user, 3000’ configuration.

Adjusting the future reach of the schedulers, $N$, while
keeping the window lengths fixed gives a marginal increase in
JFI and decrease in capacity which almost balance each other
out in CFP. The slight JFI increase results from allowing the
future schedulers to select lower-rate users ‘now’ by knowing
that other users will be selected over a longer future horizon.
The dip in capacity for the TXA scheduler is caused by the
competing manners of those two schedulers as $N$ grows,
without the stronger, compensating effect of the $t_c$ and $t_f$
scheduling windows also changing.

V. SUMMARY

This paper has presented a new scheduling methodology
based on access to the future data rates of users in a multi-
user scheduling problem. Based on modifying the PFS metric to include weighted measures of future rates, or by sliding the PFS forward into the future, a range of new scheduler options were introduced, and their performance and characteristics studied by simulation of a MIMO-OFDMA wireless system. It was shown that the future-based schedulers permit a number of capacity--fairness tradeoffs, with the ability in particular to improve usefully on the fairness of the classical PFS via the FWN and FWN+TXA schedulers.

With the dependence on future, and thus uncertain information, a clear avenue for further work is to include the impact of incorrect prediction on the future-based schedulers, a problem considered also in [7], [9], [11]. Within the context of the ViewNet project, since this is producing a functioning hardware system, it would be instructive to use real measurements of throughput tied to position to provide data to the simulators.

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REFERENCES

[1] M. C. Lawton and J. P. McGeehan, “The application of a deterministic ray launching algorithm for the prediction of radio channel character-


[18] J. Medbo and P. Schramm, Channel Models for HIPERLAN/2, ETSI BRAN document no. 3ERI086B.