
Preprint (usually an early version)
Link to published version (if available):
10.1103/PhysRevB.89.205104

Link to publication record in Explore Bristol Research
PDF-document

University of Bristol - Explore Bristol Research

General rights

This document is made available in accordance with publisher policies. Please cite only the published version using the reference above. Full terms of use are available: http://www.bristol.ac.uk/pure/about/ebr-terms.html

Take down policy

Explore Bristol Research is a digital archive and the intention is that deposited content should not be removed. However, if you believe that this version of the work breaches copyright law please contact open-access@bristol.ac.uk and include the following information in your message:

• Your contact details
• Bibliographic details for the item, including a URL
• An outline of the nature of the complaint

On receipt of your message the Open Access Team will immediately investigate your claim, make an initial judgement of the validity of the claim and, where appropriate, withdraw the item in question from public view.
Nodal Landau Fermi-Liquid Quasiparticles in Overdoped La$_{1.77}$Sr$_{0.23}$CuO$_4$


1 Institute for Condensed Matter Physics, École Polytechnique Fédérale de Lausanne (EPFL), CH-1015 Lausanne, Switzerland
2 Laboratory for Solid State Physics, ETH Zürich, CH-8093 Zürich, Switzerland
3 KIT Royal Institute of Technology, Materials Physics, LPMCN, CNRS, UMR 5586, Université Lyon 1, F-69622 Villeurbanne, France
4 Laboratory for Neutron Scattering, Paul Scherrer Institut, CH-5232 Villigen, Switzerland
5 Swiss Light Source, Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland

Nodal angle resolved photoemission spectra taken on overdoped La$_{1.77}$Sr$_{0.23}$CuO$_4$ are presented and analyzed. It is proven that the low-energy excitations are true Landau Fermi-liquid quasiparticles. We show that momentum and energy distribution curves can be analyzed self-consistently without quantitative knowledge of the bare band dispersion. Finally, by imposing Kramers-Kronig consistency on the self-energy $\Sigma$, insight into the quasiparticle residue is gained. We conclude by comparing our results to quasiparticle properties extracted from thermodynamic, magneto-resistance, and high-field quantum oscillation experiments on overdoped Tl$_2$Ba$_2$CuO$_{6+\delta}$.

I. INTRODUCTION

The extent to which Landau Fermi-liquid theory, and its concept of quasiparticles, applies to the normal state of cuprates is still under debate. Evidence for Landau Fermi-liquid quasiparticles has been reported by resistivity experiments on highly overdoped La$_{2-x}$Sr$_x$CuO$_4$ (LSCO). More recently, unambiguous proof has been given by high-field quantum oscillation experiments on both overdoped and underdoped cuprates. It is, however, puzzling that no evidence of Landau Fermi-liquid quasiparticle excitations has been found from angle resolved photoemission spectroscopy (ARPES), that is a direct probe of the Green’s function: $-(1/\pi)\text{Im}G(k,\omega)$. Although the “quasiparticles” terminology is widely used to describe the excitations of the photoemission spectra, it has never been proven by ARPES that the low-energy excitations in the cuprates are indeed true Landau Fermi-liquid quasiparticles. A direct spectroscopic proof of true Landau Fermi-liquid quasiparticles in the cuprates is therefore important.

This paper has two main objectives. The first is to prove that the nodal excitations observed in overdoped LSCO by ARPES are genuine Landau Fermi-liquid quasiparticles. The second is to discuss the nodal bare band velocity, $v_b$, and the nodal quasiparticle residue $Z \equiv <1 - \partial \Sigma/\partial \omega>^{-1}$, where $\Sigma$ is the self-energy. Perhaps the most compelling spectroscopic proof of Landau quasiparticles is the demonstration of a low-energy self-energy that has (1) the form $\Sigma'' \propto i\omega$ and (2) $-2\Sigma'' \propto \omega^2$. Proving this requires full knowledge about $\Sigma$ and insight into the bare band $\varepsilon_b$, that is not straightforward to derive from an ARPES spectrum. Here, we however present an experimental case where $Z\Sigma''$ can be evaluated without quantitative knowledge of $\varepsilon_b$. In this specific case, it is therefore possible to prove the existence of true Landau Fermi-liquid quasiparticle excitations.

II. METHODS

Nodal ARPES spectra of overdoped La$_{1.77}$Sr$_{0.23}$CuO$_4$ ($T_c = 25$K) were recorded at the surface and interface spectroscopy (SIS) beam line of the Swiss Light Source (SLS) at the Paul Scherrer Institute, Switzerland. High quality nodal spectra were obtained after cleaving at $T = 15$ K under ultra-high vacuum conditions ($p \sim 10^{-11}$ mbar). Using 55 eV circular polarized photons and a SCIENTA 2002 electron analyzer, angular and energy resolutions corresponding to 0.15° (FWHM) and $\sigma = 9$ meV (standard Gaussian deviation) were achieved. A detailed description of the experimental conditions can be found in Ref. 20.

III. RESULTS

Fig. 1(a) shows a colormap $I$ vs $(k,\omega)$ of ARPES spectra recorded close to the nodal direction of overdoped La$_{1.77}$Sr$_{0.23}$CuO$_4$. A selection of corresponding momentum distribution curves (MDC) and energy distribution curves (EDC) are displayed in Fig. 1(b,c). We start by discussing the MDCs. As this paper focuses entirely on the low-energy excitations, MDCs are only shown up to the energy scale (80 meV) of the nodal kink shown in the inset of Fig. 1(c). In this energy interval, the MDC line shapes are symmetric peaks on a constant background. Therefore, data at constant $\omega$ were analyzed using a Lorentzian function $I_0\Gamma/[(\omega - \varepsilon_0)^2 + \Gamma^2]$, where $\Gamma$ is the linewidth (Fig. 2a), $\varepsilon_0$ is the peak position (Fig. 2b), and $I_0$ is an amplitude (Fig. 3). The observed nodal excitations disperse with a Fermi velocity $v_F = 1.62(2)$ eVÅ [Fig. 2(b)], consistently with previous reports on LSCO. The half-width half-maximum, $\Gamma$, is plotted as a function of excitation energy squared $\omega^2$ in Fig. 2(a). We find that, for $\omega < \omega_c = 0.18 \pm 0.2$ eV, the linewidth is well described by $\Gamma = \Gamma(0) + \eta \omega^2$ with $\eta = 0.05 \pm 0.05$.
FIG. 1: (a) Nodal ARPES spectra recorded from overdoped LSCO ($x = 0.23$), at $T = 15$ K with 55 eV photon. The intensity, displayed versus momentum $k - k_F$ (horizontal) and excitation energy $\omega$ (vertical), has a false color scale with white as the most intense as indicated by the colorbar. (b) Momentum distribution curves (MDCs) of the spectra shown in (a), for fixed energies as indicated. Solid lines are Lorentzian fits to the data. (c) Energy distribution curves (EDCs) recorded at momenta as indicated. A $\omega$-dependent background defined by the EDC at $k - k_F = 0.089 \text{ Å}^{-1}$ (indicated by the vertical white dashed line in (a)) has been subtracted. Solid lines display the $\omega$-dependence of Eq. 3, multiplied with the Fermi-Dirac distribution and convoluted with the instrumental resolution. For the sake of visibility, data in (b) and (c) are arbitrarily shifted in the vertical direction. The insert of (c) displays the excitation dispersion derived from MDC analysis of the spectra in (a).

To reveal the intrinsic physical line shape, a background has been subtracted from the EDCs shown in Fig. 1(c). The energy dependent background was extracted from the spectra using an energy distribution curve on the unoccupied side of the dispersion (indicated by a vertical dashed line in Fig. 1(a)). This is a common procedure and an example of a raw background spectrum can be found in the supplement of Ref. 20. In this fashion, EDCs recorded at a momentum $|k|$ larger than the Fermi momentum $|k_F|$ [displayed with open circles in Fig. 1(c)] are featureless, demonstrating the successful background subtraction. On the other hand, EDCs with $k < k_F$ [full circles] reveal the intrinsic line shape of the excitations.

IV. DISCUSSION

The measured ARPES intensities $I(k, \omega)$ can be modelled by a product of the spectral function $A(k, \omega) = -(1/\pi) \text{Im} G(k, \omega)$, a matrix element $M(k, \omega)$, and the Fermi distribution $f(\omega)^{10}$. Matrix elements typically vary weakly as a function of $(k, \omega)$. Notice that the excitations shown in Fig. 1(b) disperse over less than 10 percent of the Brillouin zone. It is therefore not unreasonable to ignore matrix element effects. In that case, the ARPES intensity becomes a direct measure of the occupied part of the spectral function. It is common practice to separate the spectral function into coherent and incoherent parts, i.e., $A(k, \omega) = A_{coh}(k, \omega) + A_{inc}(k, \omega)^{10}$. The coherent part can be written as:

$$A_{coh}(k, \omega) = \frac{-1}{\pi} \frac{\Sigma'(k, \omega)}{(\omega - \Sigma'(k, \omega) - \varepsilon_b)^2 + \Sigma''(k, \omega)^2}$$

(1)

where $\varepsilon_b$ is the a priori unknown bare band, and the self-energy must obey $|\Sigma'| \gg |\Sigma''|^{1/2}$. Experimentally, one would associate sharp dispersing features to the coherent

$\eta = 3.14(4) \text{ eV}^{-2} \text{Å}^{-1}$, and $\Gamma(0) = 0.0117(1) \text{ Å}^{-1}$. The elastic scattering $\Gamma(0)$ is lower than what is usually reported for LSCO. As impurity scattering is one source of elastic scattering, low values of $\Gamma(0)$ may be an indication of high sample quality.
nondimensional region, this is a good approximation. As shown in Fig. 2, both the band velocity and MDC line width are essentially identical for the two different nodal cuts. Another indication that $\Sigma$ is momentum independent stems from the symmetric MDC lineshape shown in Fig. 1b. A $k$-dependence of $\Sigma$ along the cut-direction would lead to an asymmetric lineshape. As this is not observed, it is concluded that $\Sigma$ is locally independent of momentum both along and perpendicular to the cut direction.

It is thus possible to rewrite the coherent part of the spectral function as:

$$A_{coh}(k, \omega) = -\frac{1}{\pi} \frac{\Sigma''(\omega)}{(\omega - \Sigma'(\omega) - v_F(k - k_F))^2 + \Sigma''(\omega)^2}.$$  \hfill (2)

Notice that this is nothing else than a Lorentzian function in momentum space, with half-width half-maximum $\Gamma$ given by $\Gamma(\omega) = -\Sigma''(\omega)/v_F$. Experimentally, it is found that $\Gamma \propto \omega^2$ (see Fig. 2). Therefore, consistently with true Fermi liquid quasiparticle excitations, we conclude that $\Sigma'' \propto \omega^2$.

A Kramers-Kronig consistent self-energy with $\Sigma'' \propto \omega^2$ has $\Sigma' \propto -\gamma \omega$ in the low-energy limit. The unknown constant $\gamma$ is sometimes referred to as the quasiparticle renormalization factor. If consistency between MDC and EDC poles (dispersions) is enforced, then $1/(1 + \gamma) = v_F/v_b = Z$. The coherent spectral function can consequently be re-written as:

$$A_{coh}(k, \omega) = \frac{Z}{\pi} \frac{v_F \Gamma}{(\omega - v_F(k - k_F))^2 + (v_F \Gamma)^2},$$ \hfill (3)

where both $v_F$ and $\Gamma$ are known from the MDC analysis. The only unknown parameter, $v_b$, is a prefactor. It is therefore possible to model the EDC lineshape without quantitative knowledge of the bare band $v_b$, and with the peak amplitude as the only free parameter – see solid lines in Fig. 1(c). In the displayed energy interval, a consistent description of both EDCs and MDCs were obtained from $A_{coh}(k, \omega)$.

Because $Z = v_F/v_b$ and $\Sigma'' = -\eta v_b \omega^2$, the product $Z \Sigma'' = -v_F \eta \omega^2$ can be evaluated without quantitative knowledge of the bare band velocity. The condition for coherent quasiparticle excitations is $-Z \Sigma'' < |\omega|^{1/2}$. Using the experimental values of $v_F$ and $\eta$, we find that Landau quasiparticles are coherent for $\omega < 1/v_F \eta \sim 0.19$ eV. This energy scale is comparable to $\omega_c$ - the energy scale below which $\Sigma'' \propto \omega^2$ - and hence re-enforces the interpretation of $\omega_c$ as an energy scale related to the break down of Landau Fermi-liquid quasiparticle excitations.

Finally, we discuss the Kramers-Kronig relation between $\Sigma'$ and $\Sigma''$:

$$\Sigma' = \frac{P \int_{-\omega_c}^{\infty} \Sigma''(\omega') d\omega'}{\pi} + \frac{P \int_{-\omega_c}^{\omega} \Sigma''(\omega') d\omega'}{\pi} \quad \left(4\right)$$

where $P$ is the principal value and $W$ is the band width. To first order, the quasiparticle part yields $\Sigma_{qp} \simeq \gamma_{qp} \omega$.  

FIG. 2: (a) Linewidth $\Gamma$ of the momentum distribution curves plotted versus excitation energies squared ($\omega^2$), for the two cuts shown in the inset of (b). Inset of (a) shows $\Gamma$ vs $\omega$. The deviation from $\omega^2$ dependence defines the energy scale $\omega_{coh}$ indicated by the arrow. (b) Nodal dispersions extracted from MDC analysis for the two cuts shown in the inset. The dashed line indicates the bare-band extracted by assuming Kramers-Kronig consistency of the self-energy $\Sigma$, see text. The inset shows the Fermi surface of LSCO $x = 0.23$ and the two cuts along which the spectra were recorded.
where \( \gamma_{qp} = 2v_F p \omega_c / \pi \). To gain insight into \( \Sigma_{\text{qp}} \), we define \( Z_i(\omega) = (1 - \partial \text{Re} \Sigma_i / \partial \omega)^{-1} \) so that \( Z(\omega) = Z_{\text{qp}}(\omega) + Z_{\text{qp}}(\omega) \). As \( Z(\omega) \approx I_0(\omega) \) varies weakly with excitation energies (see Fig. 3), we infer that \( Z_{\text{qp}} \) (to first order) is \( \omega \)-independent. Hence \( \text{Re} \Sigma_{\text{qp}}(\omega) = \gamma_{\text{qp}} \omega \) and \( Z = 1/(1 + \gamma_{\text{qp}} + \gamma_{\text{qp}}) \). As long as the detailed high-energy part of \( \text{Im} \Sigma(\omega) \) is unknown, it is not possible to directly extract \( \gamma_{\text{qp}} = \gamma_{\text{qp}} \omega \). This is known as the "tail" problem. The linear \( \omega \)-dependence at high-energies, shown in the inset of Fig. 2, yields \( \gamma_{\text{qp}} \sim \ln(C/\omega_c) \) where \( C \) is an unknown constant. Hence \( \gamma_{\text{qp}} \) diverges only logarithmically in the limit \( \omega_c \to 0 \). On the other hand, for large \( \omega_c \), the role of \( \gamma_{\text{qp}} \) will be less important. As \( \omega_c \), \( 0.18 \) eV is a large energy scale, corresponding to a temperature scale of the order 1000 K, we hypothesize that \( \gamma_{\text{qp}} \ll 1 \). In that case, \( Z \approx 1/(1 + \gamma_{\text{qp}}) = v_F / v_b \) and hence \( v_b = \pi v_F / (\pi - 2 \omega_c v_F) \approx 3.8 \) Å. This is consistent with the nodal LDA Fermi velocity \( v_{LDA} = 3.5 \) eV Å calculated for LSCO and with values of \( v_b \) derived from a numeric self-consistent method. The consistent values of \( v_b \) further support the conjecture that \( \gamma_{\text{qp}} \ll 1 \).

The quasiparticle mass is given by \( m_b / m_* = Z \tilde{Z} \), where \( m_b \) is the bare mass and \( Z = 1 + \left(m_b / h^2 k_F \right) \partial \Sigma'(k, 0) / \partial k_\perp^{17,31} \). Since the self-energy is locally independent of momentum, the nodal quasiparticle mass is given by \( m_* = m_b / Z \approx 2.4 m_b \). This is comparable to the momentum averaged values \( m_* \approx 3 m_b \) extracted from quantum oscillations and electronic specific heat experiments on overdoped \( \text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta} \) \( \text{(Tl2201)}^{15} \). Remarkably, a Fermi-liquid cut-off energy scale \( \omega_c \approx 0.2 \) eV was extracted from angle-dependent magneto-resistance measurements on overdoped Tl2201. This is in good agreement with nodal ARPES spectra recorded on LSCO \( x = 0.23^{22} \). On LSCO, no quantum oscillation or angle-dependent magneto-resistance experiments exist. Insight into the average quasiparticle mass of overdoped LSCO stems, therefore, alone from specific heat measurements. Compared to Tl2201, a somewhat larger Sommerfeld constant \( \gamma_{el} \approx 12 \) mJ/(mole K²) is found for overdoped LSCO \( x \approx 0.23^{22} \), suggesting a larger average quasiparticle mass. This is not necessarily inconsistent with the ARPES data. The Fermi-liquid cut-off energy scale, \( \omega_c \), softens rapidly as a function of Fermi surface angle, and the quasiparticle scattering is globally dependent on momentum. This implies (1) that the contribution from non-Fermi liquid excitations will become increasingly important and (2) that \( \tilde{Z} < 1 \) on certain portions of the Fermi surface. Both effects would lead to larger quasiparticle masses.

V. CONCLUSIONS

In summary, we have proven that the nodal single particle excitations observed by ARPES in overdoped LSCO are indeed true Landau Fermi liquid quasiparticle excitations. This result, together with consistent MDC and EDC analysis, was obtained without knowing the exact bare band. From Kramers-Kronig consistency of the quasiparticle self-energy \( \Sigma \), insight into the bare band \( e_b \) and the real part of the self-energy \( \Sigma' \) were obtained. An estimate of the nodal quasiparticle residue \( Z = 0.42^{(7)} \) allowed comparison to quasiparticle masses obtained from thermodynamic and high-field quantum oscillation experiments on overdoped \( \text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta} \) compounds.

Acknowledgments: This work was supported by the Swiss NSF (through NCCR, MaNEP, and grant Nos. 200020-105151 and PZ00P2-142434), the Ministry of Education and Science of Japan, and the Swedish Research Council. The experimental work was performed at the SLS of the Paul Scherrer Institut, Villigen PSI, Switzerland. We thank the X09LA beamline staff for their technical support.

6. B. Vignolle, A. Carrington, R. A. Cooper, M. M. J. French,


There are at least two ways to mimic the effect of instrumental resolution. One is to use the measured $\Gamma_0$ and the width of the Fermi step that already include instrumental resolution. Another method is to use $\Gamma_0(\text{intrinsic}) = (\Gamma_k^2 - \Gamma_k(\text{res})^2)^{0.5}$, where $\Gamma_k(\text{res})$ is the momentum resolution, a Fermi step defined by $k_B T$ and then convolve this with the instrumental resolution. Both methods where tried with essentially identical results.


